MMCC '14 P3 - Esdeath

Time limit: 0.6s   **Memory limit:** 64M

Mini March Coding Challenge 2014

Esdeath is excited — she has information that Tatsumi will be appearing today in one of N cities, conveniently labeled from 1 to N. The Prime Minister (Esdeath's boss) does not care much for the citizens, so there are only $N - 1$ bidirectional roads connecting the cities, and all cities are connected to every other city by just one path. Because Esdeath does not want Tatsumi to escape unnoticed, she has brought her army in to wait for him. Esdeath's army has S soldiers, and she would like to station the soldiers at S of the N cities such that no matter which city Tatsumi appears in, the minimum distance from any soldier to Tatsumi will be no greater than D roads. As one of Esdeath's pets, you'll be rewarded if you can help her find the minimum value of D — so do so, and quickly!

Input Specification

The first line of input has 2 integers, N and S ($1 \leq S \leq N \leq 5000$), the number of cities and the number of soldiers in Esdeath's army, respectively. Each of the next $N - 1$ lines contain two integers u_i and v_i, representing a bidirectional road between cities u_i and v_i.

The following additional constraints will apply.

- At least 15% of the marks will be for test cases where $N \leq 100$ and $S = 1$;
- At least 30% of the marks will be for test cases where $N \leq 100$ and $S \leq 10$;
- At least 50% of the marks will be for test cases where $N \leq 250$ and $S \leq N$;
- The remaining marks will be for test cases where $N \leq 5000$ and $S \leq N$.

Output Specification
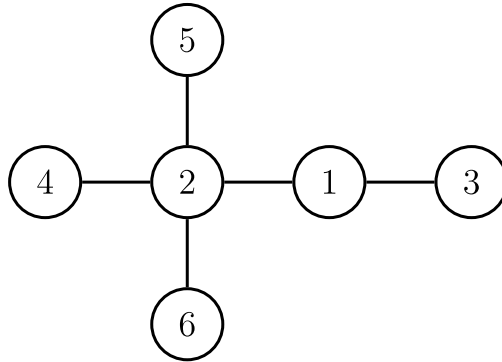
Output the minimum possible value of D.

Sample Input 1

```
6 1
1 2
2 4
2 5
2 6
1 3
```

Sample Output 1

```
2
```

Explanation for Sample Output 1

The cities and roads are laid out like the following:

Esdeath's army only consists of 1 soldier, and placing that soldier at either city 1 or city 2 will result in every city being at most 2 roads away.

Sample Input 2

```
10 3
5 3
3 10
9 1
2 1
1 5
7 10
6 7
7 8
8 4
```

Sample Output 2

```
2
```